

The background of the entire page is a close-up photograph of a butterfly wing, showing intricate patterns and colors. A digital glitch effect, consisting of horizontal lines of varying lengths and colors (red, white, black), is overlaid on the image, creating a sense of digital corruption or data interference. The text is placed over these glitched areas.

**ACADIA 2012**

**SYNTHETIC  
DIGITAL  
ECOLOGIES**

**SAN FRANCISCO // OCTOBER 18-21**

PROCEEDINGS OF THE 32ND ANNUAL  
CONFERENCE OF THE ASSOCIATION FOR  
COMPUTER AIDED DESIGN IN ARCHITECTURE  
(ACADIA)

**EDITED BY**

Mark Cabrinha, California Polytechnic State University, San Luis Obispo  
Jason Kelly Johnson, California College of the Arts, San Francisco  
Kyle Steinfeld, University of California, Berkeley

# **Fabricating Sustainable Concrete Elements: A Physical Instantiation of the Marching Cubes Algorithm**

Jesse Jackson, OCAD University and Luke Stern, Patkau Architects

## **Abstract**

This paper explores how an algorithm designed to represent form can be made physical, and how this physical instantiation can be made to respond to a set of design imperatives. Specifically, this paper demonstrates how Marching Cubes (Lorensen and Cline 1987), an algorithm that extracts a polygonal mesh from a scalar field, can be used to initiate the design of a system of modular concrete armature elements that permit a large degree of variability using a small number of discrete parts. The design of these elements was developed in response to a close examination of Frank Lloyd Wright's Usonian Automatic system, an architecturally pertinent historical precedent (Pfeiffer 2002). The fabricated results positively satisfy contemporary design criteria, including maximal formal freedom, optimal environmental performance, and minimal life-cycle costs.

## **1.0 Introduction**

Our research trajectory began with the observation that computer graphics algorithms used to subdivide a scalar field into a cubic-grid polygonal mesh might have a physical analogue in element-based construction. This led to iterative attempts to design an element-based construction assembly derived from Marching Cubes, a seminal example of this type of graphics algorithm. The validity of the most promising design was then tested through full-scale fabrication using contemporary rapid prototyping technology.

An in-depth examination of Frank Lloyd Wright's Usonian Automatic system provided an architectural context for these explorations. The Automatic system, like our proposal, also provided a rule-based means to subdivide a regular, gridded space to create form while also considering the constructional element as a design exercise in itself.

## **2.0 A Conceptual Framework: Prioritizing the Tectonic Elements**

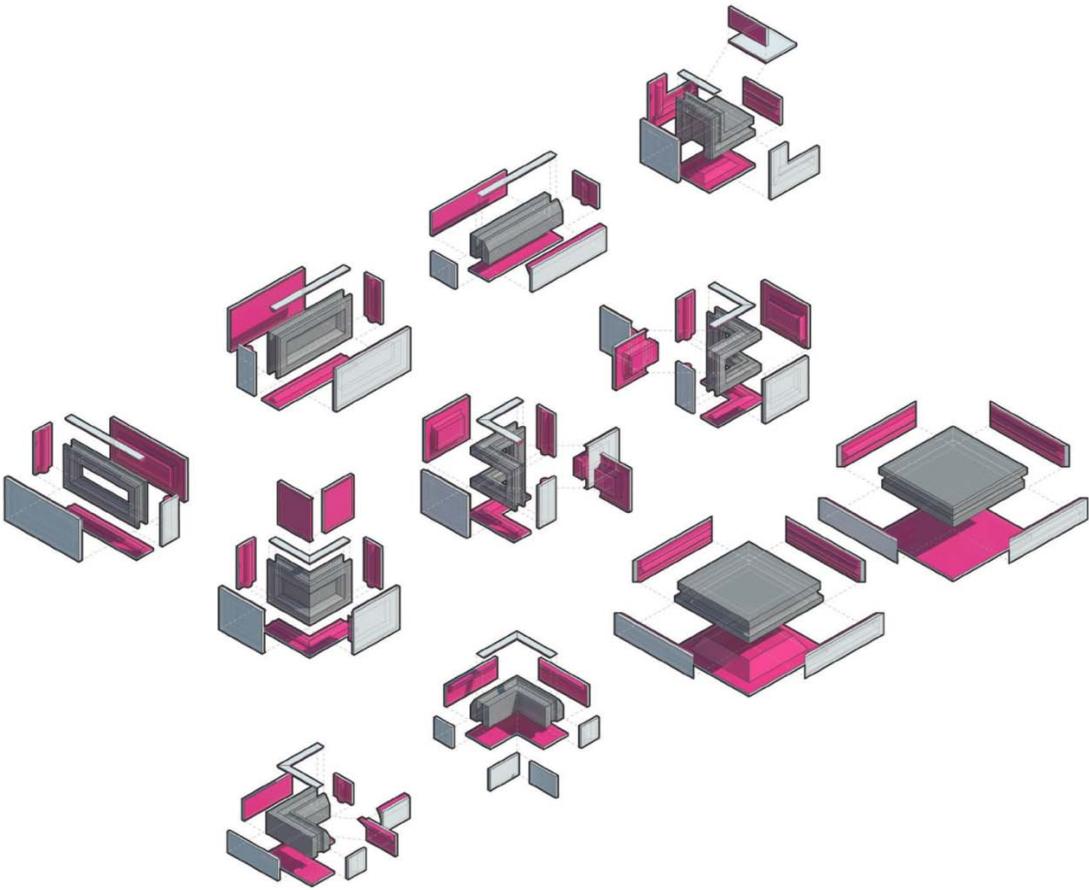
Subdivision into elements, through pixels, voxels, or tessellation, is a fundamental quality of the virtual realm. In the physical realm, the analogous unit parts are commonly referred to as the tectonic elements of built form, and are normally considered to be subordinate components of a greater architectural endeavor. These elements have desired qualities – *firmitas*, *utilitatis*, and *venustatis* – comparable to that of an aggregate assembly, and warrant direct design consideration (Frampton 1995). The parallel between virtual and physical elements was utilized in service of an original design for a unit-based system of construction.

### **2.1 A Point of Departure: Frank Lloyd Wright's Usonian Automatic System**

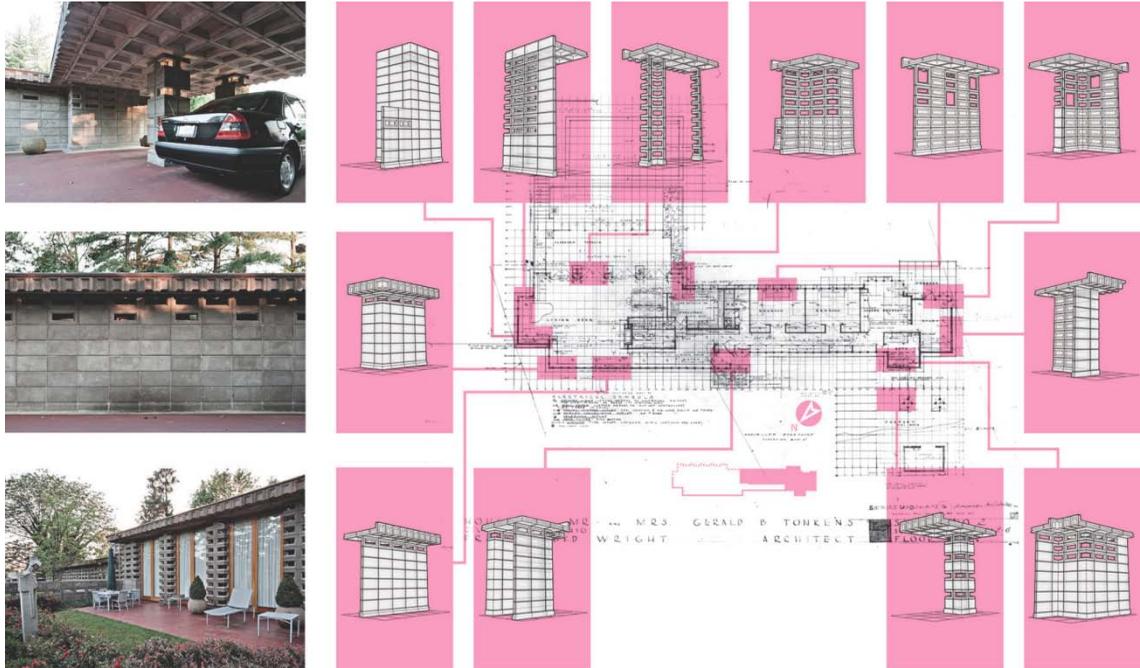
Frank Lloyd Wright's Usonian Automatic system of concrete block construction is a well-known precedent for the prioritization of the tectonic elements (Frampton 1995). Deconstruction, reconstruction and replication of this system provided a point of departure for our research. Though much of this work is outside of the scope of this paper and has been documented elsewhere (Jackson and Stern 2009), it is summarized here for context.

Wright used the term Usonia to denote his vision for a new American landscape characterized by a diffuse agrarian urbanism. In particular, Usonian refers to a series of modest family homes featuring native materials, flat roofs, and large cantilevered overhangs. Early Usonian homes used a wood board-and-batten construction technique, but faced with rising labour costs in the 1950s, Wright turned to concrete. The term Automatic was adopted because the revised design created the potential for end-user assembly and therefore economy, facilitated by a strict grid that determined the dimensions and relative positions of the constituent concrete elements. These elements can be seen as miniature manifestations of the buildings they create, each with a sense of mass and texture that continues to be evident in the assembled whole.

Figures 1-4 below illustrate some of the key results of our deconstruction, reconstruction and full-scale replication process.



**Figure 1: Frank Lloyd Wright's Automatic elements**



**Figure 2: In-situ use of the Automatic elements**



**Figure 3: Reconstruction of the Automatic formwork**



**Figure 4: Full-scale replication of the Automatic system**

### **3 Design Imperatives**

This detailed examination of the Automatic system helped situate our research in an architectural context, and began to suggest design imperatives that would inform the new design proposal, including:

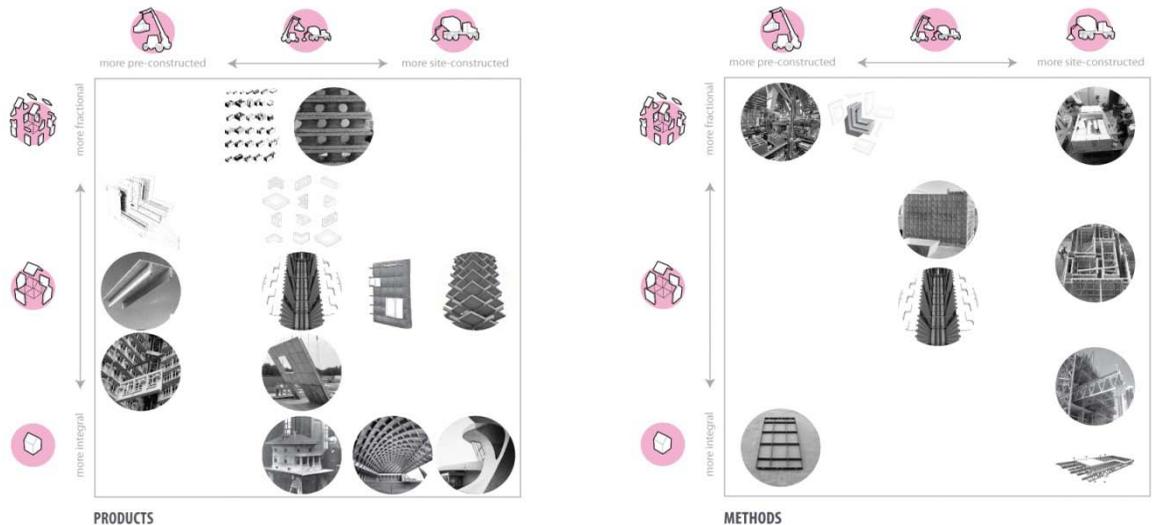
- innovative concrete materiality;
- environmental, cultural and economic sustainability; and
- element connectivity and specificity.

#### **3.1 Innovative concrete materiality**

We anticipated that our new design proposal would continue to be made of concrete. Concrete products can be categorized by the degree to which they are either site-constructed or pre-constructed, and by the degree to which they are elemental in nature. An analysis of historical and contemporary concrete assemblies was conducted, including: everyday concrete masonry units; autoclaved aerated concrete building systems (Rastra); proprietary composite insulated concrete panels; contemporary designer concrete elements (Loom); and, of course, Usonian Automatic blocks. Given that concrete always begins in a liquid state, the methods required to fabricate each assembly were also of interest and were similarly investigated, including: conventional one-off wood forms; fly-forms; and deck systems; modular plastic formwork (Moladi); and more unconventional techniques, such

as Edison's single pour system (Bergdoll 2008).

These analyses, summarized in Figure 5, helped position our new design within the spectrum of concrete construction practices, with the specific aim of identifying opportunities for innovation and how existing systems failed to address our design imperatives. Notably, many of the existing systems failed to overcome: a) their pre-determined orientation, because their structure and form reflect the forces they will be subjected to, and b) the inherent tension between simplicity and specificity, by subscribing to one of the "one-size-fits-all" or mass-customization extremes.



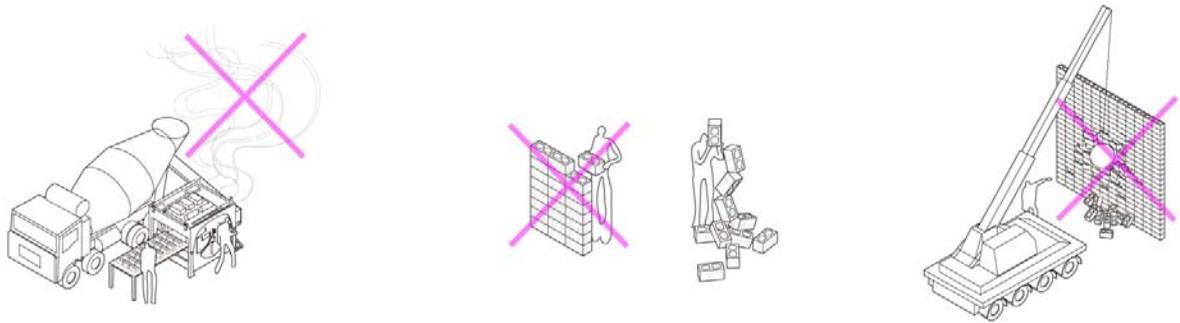
**Figure 5: Concrete products and methods**

### 3.2 Environmental, Cultural and Economic Sustainability

Wright's system was designed when resources were believed to be infinite. Given our acknowledgement that resources are indeed finite, we sought to make our proposal respond to contemporary environmental, cultural, and economic sustainability concerns, including:

- Impact mitigation: employing advancements in constituents and techniques that mitigate some of the deleterious effects of concrete production.
- Formal flexibility: providing maximal freedom of expression.
- Life-cycle optimization: maximizing the potential for reuse - typical concrete elements require permanent assembly methods that inhibit reuse.

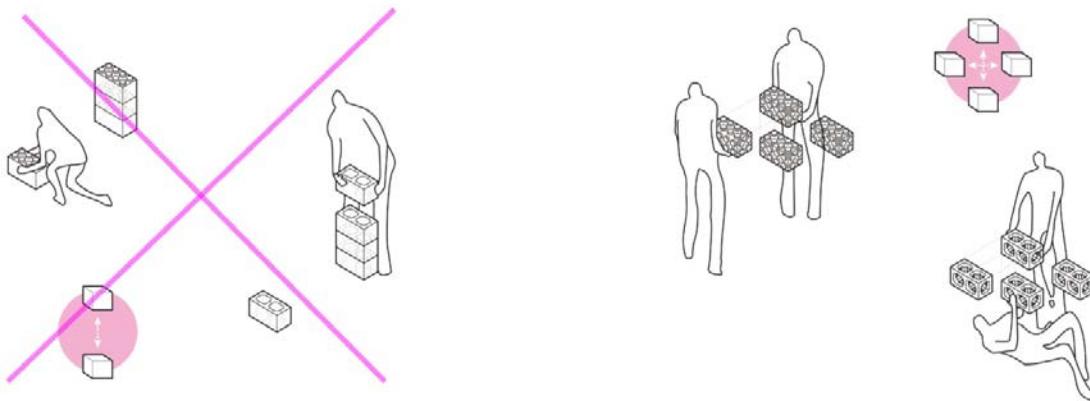
These imperatives are represented in Figure 6.



**Figure 6: Sustainability imperatives**

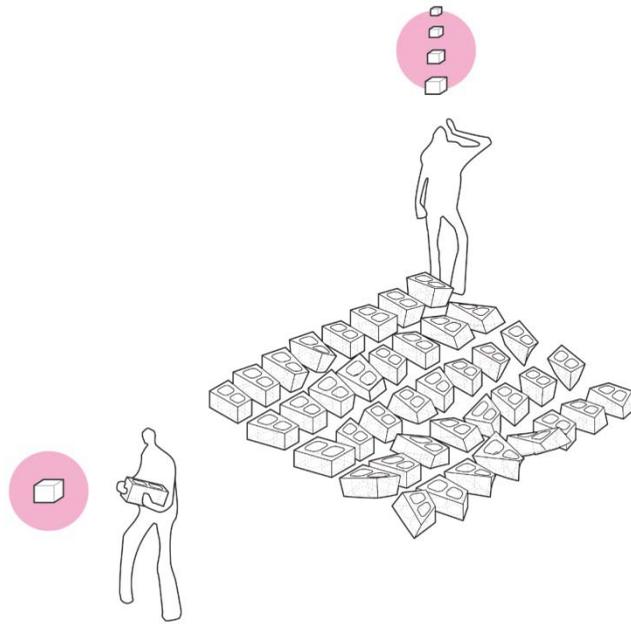
### 3.3 Element Connectivity and Specificity

Like Lego™, both Wright's system and conventional concrete blocks are designed with a specific orientation and position in mind. In order to achieve more formal flexibility, the new proposal was designed to permit universal connectivity to facilitate both stacking and spanning, as shown in Figure 7.



**Figure 7: Universal connectivity**

The design also sought to permit the freedom to generate a significant range of forms while remaining simple enough to understand and organize. An important parameter in this potentially conflicting desire, represented by Figure 8, is the number of discrete parts: too many, and the system will become onerous to use; too few, and the system has a potentially limited application.



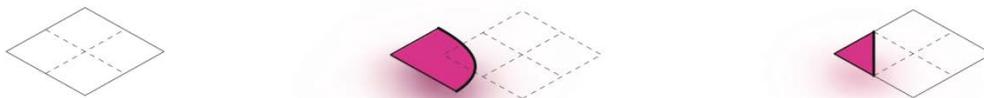
**Figure 8: Simplicity versus formal freedom**

#### **4 One Physical Instantiation of Marching Cubes**

Universal connectivity and a balance between simplicity and formal freedom can be achieved by leveraging the results of a set of form-finding rules. These rules have their origin in a pair of computer graphics algorithms developed for constructing polygonal meshes in two and three-dimensional space: Marching Squares and Marching Cubes.

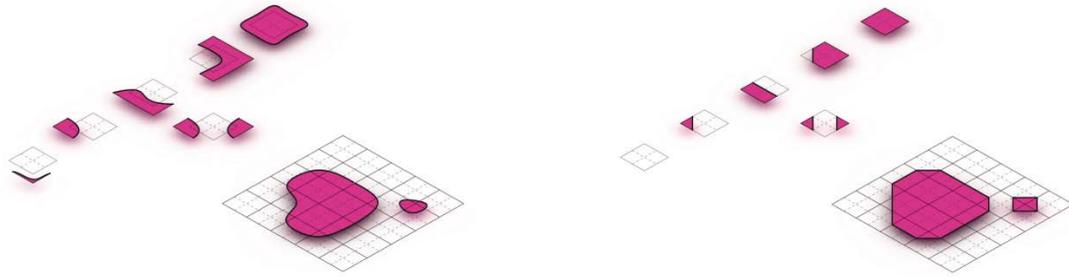
##### **4.1 Marching Squares Made Graphical**

Marching Squares can be made graphical by dividing a plane into quadrants, intersecting this plane with any arbitrary region, and finally approximating this region as shown in Figure 9. The approximation is determined by the quadrants through which the arbitrary region passes.



**Figure 9: Marching Squares made graphical**

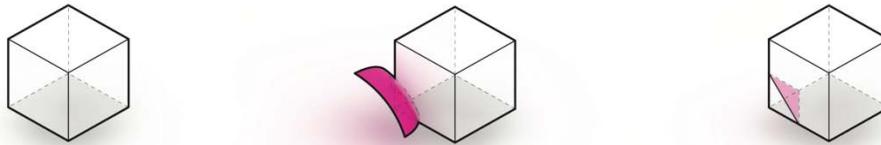
There are six quadrant/region intersections possible, each of which can be approximated and, in combination, used to approximate a closed region of any size and shape, as shown in Figure 10. The resolution of the approximation is dependent on the size of the quadrants: smaller quadrants provide higher resolution.



**Figure 10: All permutations of Marching Squares**

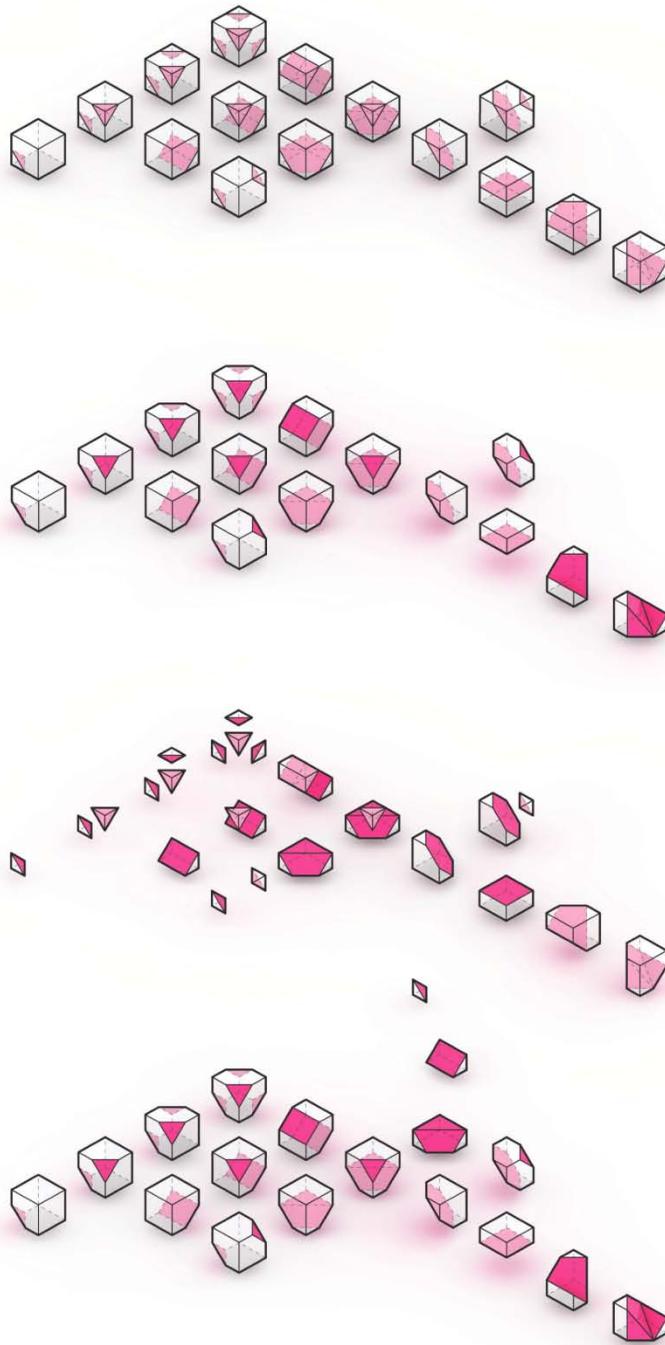
#### 4.2 Marching Cubes Made Elemental

The same logic can be applied in three dimensions in order to make Marching Cubes elemental. Any arbitrary surface, intersecting a cube divided into quadrants, can be approximated as shown in Figure 11. Again, the approximation is determined by the quadrants through which the arbitrary surface passes.



**Figure 11: Marching Cubes made elemental**

There are fifteen quadrant/surface intersection approximations possible, which can be interpreted reciprocally as either positive or negative volumes, generating eighteen unique elemental forms. These elements can be used in combination to approximate any closed surface, as shown in Figure 12. Again, smaller quadrants create more resolution.

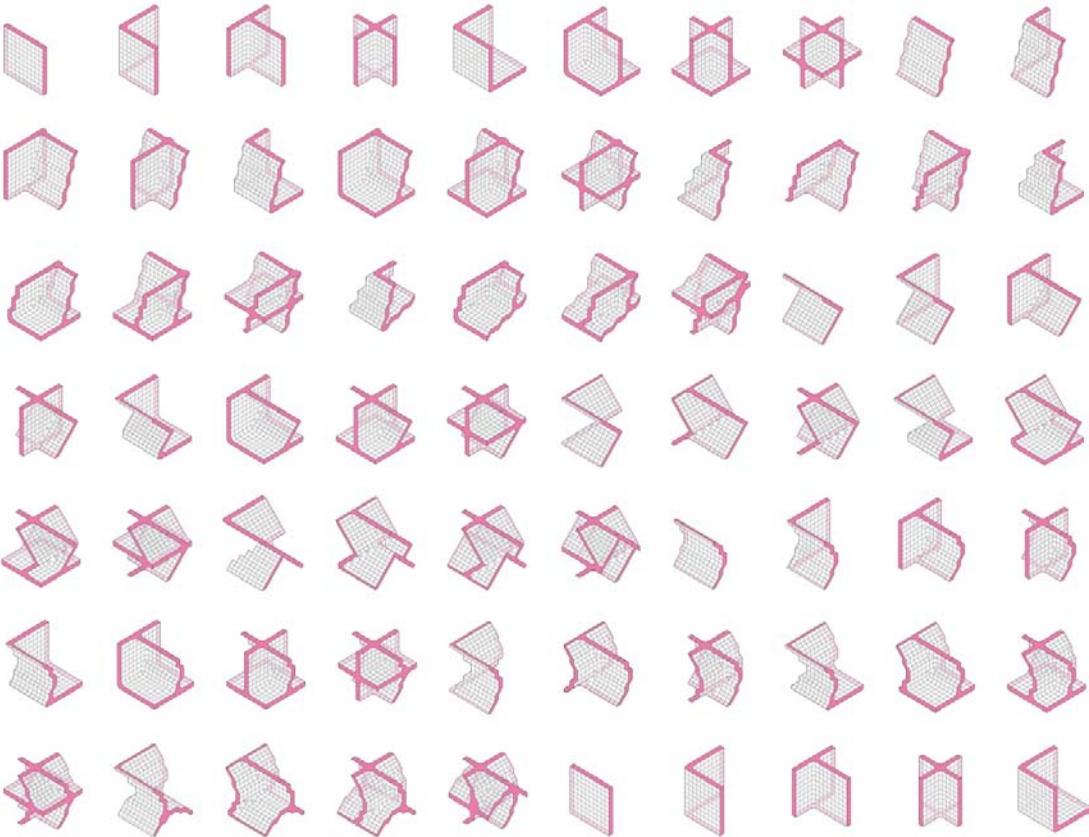


**Figure 12: All permutations of Marching Cubes made elemental**

### 4.3 The Elements Made Architectural

While the Marching Cubes algorithm can be used to approximate any surface, the eighteen unique elements can also create aggregate forms with architectural relevance. Typical enclosure configurations such as walls, floors and roofs, and intersections of the three can be produced utilizing this system of construction elements. These elements, like Wright's

Automatic blocks, encode their strong formal vocabulary and character on any design to which they are applied. Sixty-four sample aggregations, ranging from normative orthogonal configurations to more complex forms, such as kinked and curved configurations, are shown in Figure 13.

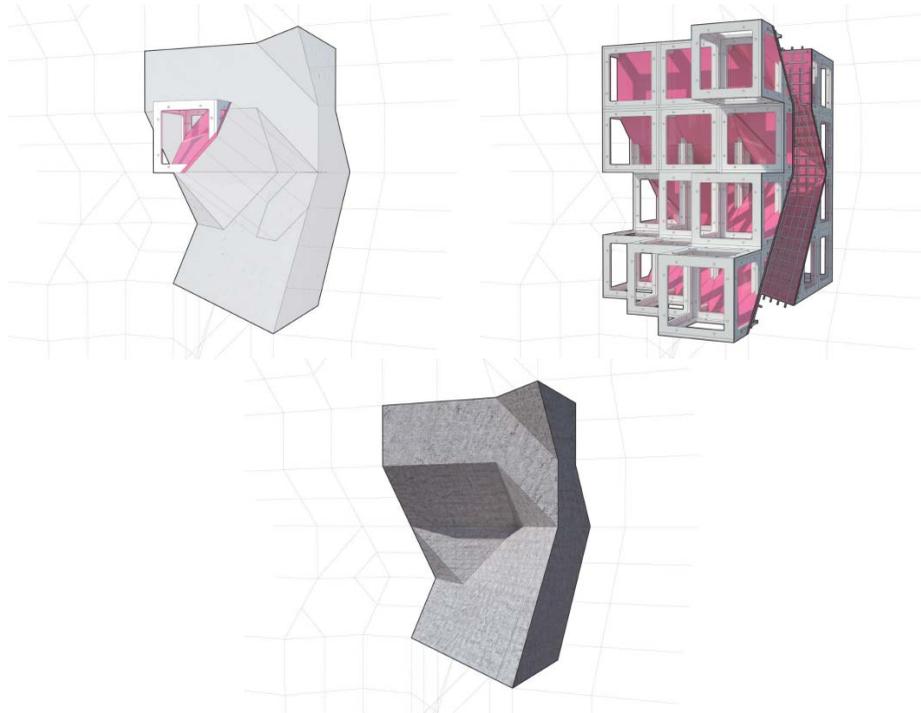


**Figure 13: Sixty-four architectural configurations**

An important parallel between the positive/negative nature of the individual elements and concrete products is that concrete products also have a reciprocal negative: the mold or formwork. When the positive is rendered in concrete, the reciprocal negative of each element becomes its formwork. Understanding this, it was possible to eliminate redundant or non-essential elements from the system, as shown in Figure 14. This reduced set of elements creates an equally complete but substantially less complex system, at the expense of the resolution of some kinked and curved configurations.

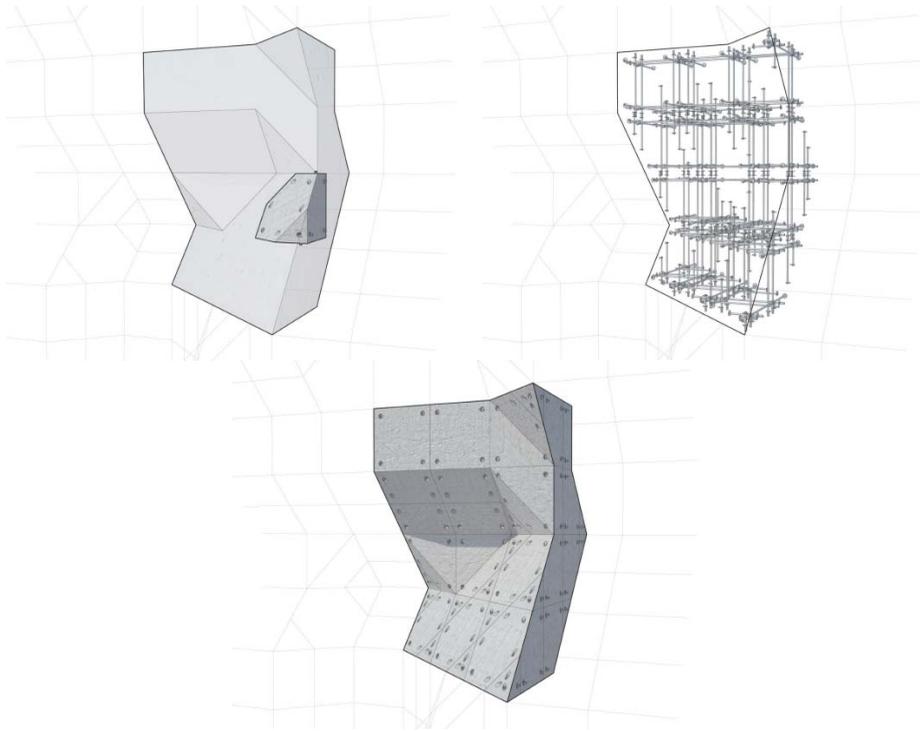


In the cast-in-place variant, shown in Figure 16, the elements become two-sided modular formwork which, when concrete is poured between them, creates an architectural enclosure. An offset grid of reinforcing steel is required on each side to resist tension, the size and quantity of which is determined by the enclosure's loading and orientation. The formwork is re-useable, permitting a small number of formwork elements to create a large variety and quantity of architectural enclosures without the difficulty and waste normally associated with the cast-in-place construction of complex geometry.



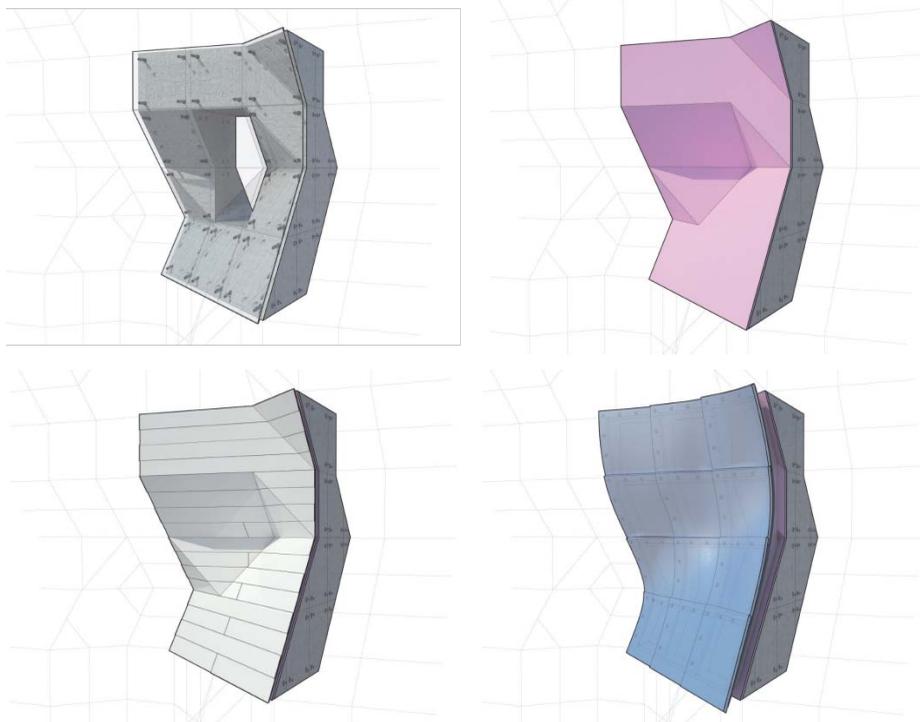
**Figure 16: Cast-in-place variant**

In the pre-cast variant, shown in Figure 17, the elements become factory produced concrete units. These units require tri-axial post-tensioning, which is provided by a system of connection rods and couplings, and which simultaneously facilitates the one-by-one assembly of the units and eliminates the need for elaborate shoring. Unlike the cast-in-place variant, the development of tensile capacity in the pre-cast variant is orientation-independent and reversible: the system can be disassembled and reassembled into new configurations as desired.



**Figure 17: Pre-cast variant**

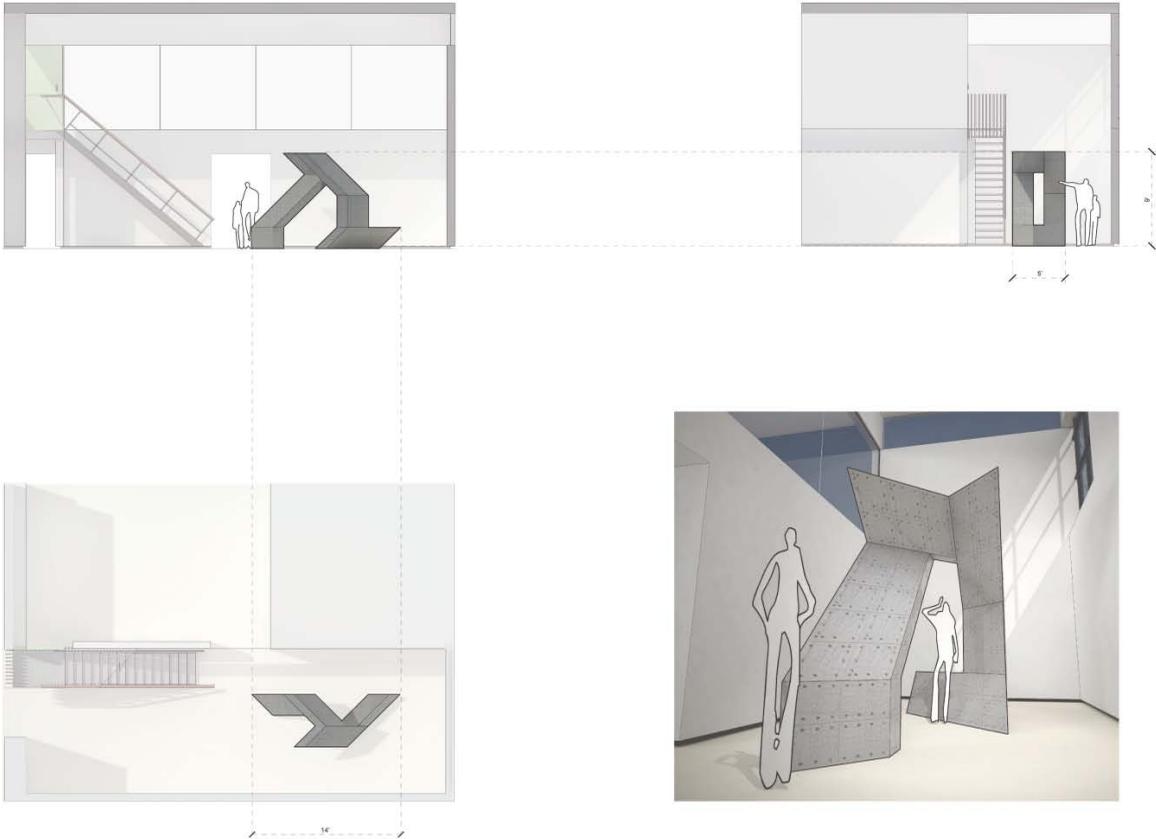
The flexible structural armature permitted by either variant offers many possibilities for cladding, including insulation, slatting, glazing and paneling, as shown in Figure 18. The armature's resolution can either be expressed directly, or can be used as a substructure.



**Figure 18: Cladding the armature**

#### 4.4 The Architecture Made Physical

Finally, a response to a specific site – a gallery – was proposed, as shown in Figure 19. The pre-cast variant was selected as the most suitable system for this temporary installation as it could be easily assembled and then demounted to be potentially re-mounted and/or reconfigured at a later time.

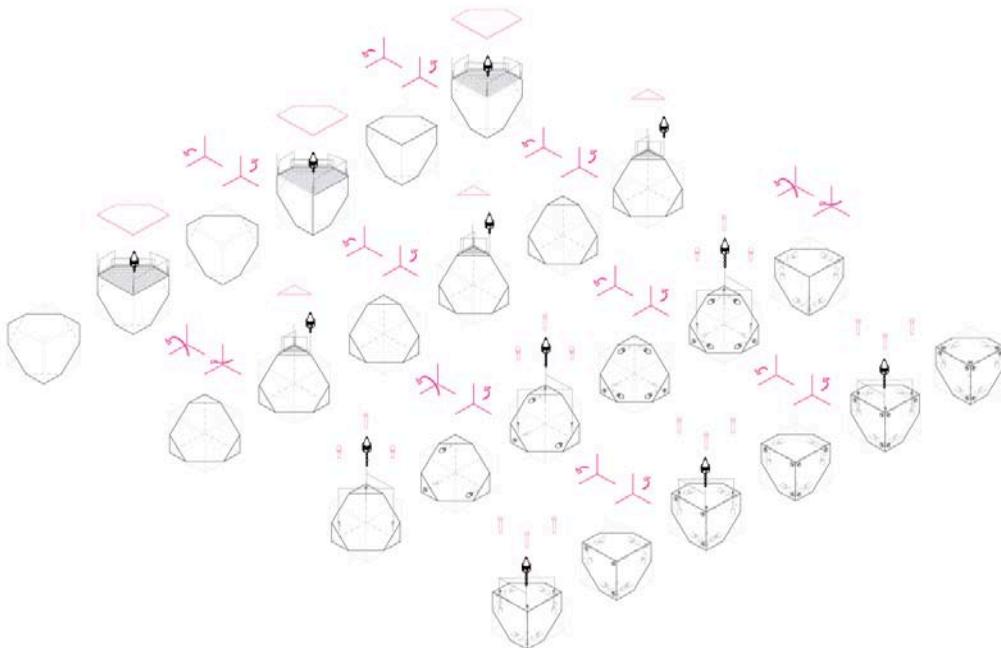


**Figure 19: Proposed gallery installation**

Figures 22-26 show aspects of the fabrication and installation process.



**Figure 20: Full-scale fabrication of the pre-cast variant**



**Figure 21: Milling procedure required to complete the pre-cast variant**



**Figure 22: Physical instantiation of the Marching Cubes algorithm**

## 5.0 Conclusions and Future Directions

The full-scale fabrication of the gallery installation revealed advantages and limitations of the design, which will be discussed in a future paper. However, two preliminary conclusions may be drawn:

- This physical instantiation of Marching Cubes, as a modular system of re-useable concrete elements that permit a large degree of formal variability using a small number of discrete parts, convincingly satisfies the established design imperatives.
- The direct consideration of constructional elements and the full-scale fabrication of those elements as a parallel exercise to conventional design activity empowers the architect to reclaim problem-solving agency (Kieran 2004).

The synergies between the digital and the physical demonstrated by this body of work validate further exploration into the translation of form-finding algorithms into material objects. The potential to leverage generative algorithms to facilitate design using these elements remains a tantalizing line of research as does the possibility of addressing non-concrete based instantiations of the elements.

## 6.0 References

- Lorensen, W and H. Cline. Marching Cubes: A high resolution 3D surface construction algorithm (paper presented at SIGGRAPH 1987: fourteenth annual Conference on Computer Graphics and Interactive Techniques, Anaheim, California, July 21–24, 1987).
- Pfieffer, B. (2002). Frank Lloyd Wright: Usonian Houses, 6-44. Tokyo: A.D.A. Editra Tokyo Co.
- Frampton, K. (1995). Studies in Tectonic Culture: The Poetics of Construction in Nineteenth and Twentieth Century Architecture, ed. J. Cava, 1-27. Cambridge: MIT Press.
- Frampton, K. (1995). Studies in Tectonic Culture, 103-120.
- Jackson, J and L. Stern, "Automatic" (exhibition at the Eric Arthur Gallery, John H. Daniels Faculty of Architecture, Landscape and Design, Toronto, Canada, January 12–23, 2009).
- Rastra. "Compound ICF." <http://www.rastra.com/> (accessed Jan 1, 2009)
- Loom. "12Block." <http://www.loomstudio.com/12blocks/> (accessed Jan 1, 2009)
- Moladi. "Low Cost Housing." <http://moladi.com/> (accessed Jan 1, 2009)
- Bergdoll, B, P. Christensen, and R. Broadhurst (2008). Home delivery: fabricating the modern dwelling, 42-47. New York: D.A.P./Distributed Art Publishers.
- Kieran, S. (2004). Refabricating Architecture : How Manufacturing Methodologies are Poised to Transform Building Construction, ed. James Timberlake, 105-132. New York: McGraw-Hill, 2004.